

# Logical clocks

### Assign sequence numbers to messages

- All cooperating processes can agree on order of events
- vs. physical clocks: time of day

### Assume no central time source

- Each system maintains its own local clock
- No total ordering of events
  - No concept of happened-when

### Happened-before

Lamport's "happened-before" notation

 $a \rightarrow b$  event *a* happened before event *b* e.g.: *a*: message being sent, *b*: message receipt

Transitive: if  $a \rightarrow b$  and  $b \rightarrow c$  then  $a \rightarrow c$ 

# Logical clocks & concurrency

Assign "clock" value to each event

- if  $a \rightarrow b$  then clock(a) < clock(b)
- since time cannot run backwards

If a and b occur on different processes that do not exchange messages, then neither  $a \rightarrow b$  nor  $b \rightarrow a$  are true

- These events are concurrent

### Event counting example

- Three systems:  $P_0, P_1, P_2$
- Events *a*, *b*, *c*, ...
- Local event counter on each system
- Systems occasionally communicate





# Lamport's algorithm

- Each message carries a timestamp of the sender's clock
- When a message arrives:
  if receiver's clock < message timestamp set system clock to (message timestamp + 1)
  - else do nothing
- Clock must be advanced between any two events in the same process

### Lamport's algorithm

Algorithm allows us to maintain time ordering among related events

- Partial ordering



### Summary

- Algorithm needs monotonically increasing software counter
- Incremented at least when events that need to be timestamped occur
- Each event has a Lamport timestamp attached to it
- + For any two events, where a  $\rightarrow$  b: L(a) < L(b)

### Problem: Identical timestamps



 $a \rightarrow b, b \rightarrow c, ...$ : local events sequenced  $i \rightarrow c, f \rightarrow d, d \rightarrow g, ...$ : Lamport imposes a send  $\rightarrow$  receive relationship

Concurrent events (e.g., a & i) <u>may</u> have the same timestamp ... or not

# Unique timestamps (total ordering)

#### We can force each timestamp to be unique

- Define global logical timestamp (Ti, i)
  - T<sub>i</sub> represents local Lamport timestamp
  - i represents process number (globally unique)
  - E.g. (host address, process ID)

- Compare timestamps:

(T<sub>i</sub>, i) < (T<sub>j</sub>, j) if and only if

- T<sub>i</sub> < T<sub>j</sub> or T<sub>i</sub> = T<sub>j</sub> and i < j

#### Does not relate to event ordering





## Problem: Detecting causal relations

#### If L(e) < L(e')- Cannot conclude that $e \rightarrow e'$

#### Looking at Lamport timestamps - Cannot conclude which events are causally related

Solution: use a vector clock

## Vector clocks

#### Rules:

- 1. Vector initialized to 0 at each process  $V_{i}[j] = 0$  for i, j = 1, ..., N
- 2. Process increments its element of the vector in local vector before timestamping event:  $V_{i}[i] = V_{i}[i] + 1$
- 3. Message is sent from process  $P_i$  with  $V_i$ attached to it
- 4. When P<sub>j</sub> receives message, compares vectors element by element and sets local vector to higher of two values
  - V\_j[1] = max(V\_i[1], V\_j[1]) for i=1, ..., N

# Comparing vector timestamps

#### Define

 $\begin{array}{l} \mathsf{V} = \mathsf{V}' \text{ iff } \mathsf{V}[i] = \mathsf{V}'[i] \text{ for } i = 1 \dots N \\ \mathsf{V} \leq \mathsf{V}' \text{ iff } \mathsf{V}[i] \leq \mathsf{V}'[i] \text{ for } i = 1 \dots N \end{array}$ For any two events e, e' if  $e \rightarrow e'$  then V(e) < V(e') • Just like Lamport's algorithm if V(e) < V(e') then  $e \rightarrow e'$ 

Two events are concurrent if neither  $V(e) \leq V(e')$  nor  $V(e') \leq V(e)$ 























# Summary: Logical Clocks & Partial Ordering

- Causality
  - If *a->b* then event *a* can affect event *b*
- Concurrency
  - If neither a->b nor b->a then one event cannot affect the other
- Partial Ordering
  - Causal events are sequenced
- Total Ordering
  - All events are sequenced

